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### Semester Two Examination, 2017

### Question/Answer booklet

# MATHEMATICS

If required by your examination administrator, please place your student identification label in this box

**SPECIALIST**

**UNITS 1 AND 2**

## Section Two:

## Calculator-assumed

|  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| Student Number: In figures |  |  |  |  |  |  |  |  |  |  |

In words

Your name

## Time allowed for this section

Reading time before commencing work: ten minutes

Working time: one hundred minutes

## Materials required/recommended for this section

***To be provided by the supervisor***

This Question/Answer booklet

Formula sheet (retained from Section One)

***To be provided by the candidate***

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in this examination

## Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

## Structure of this paper

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Section | Number of questions available | Number of questions to be answered | Working  time (minutes) | Marks available | Percentage of examination |
| Section One:  Calculator-free | 8 | 8 | 50 | 52 | 35 |
| Section Two:  Calculator-assumed | 13 | 13 | 100 | 98 | 65 |
|  | | |  | **Total** | 100 |

|  |  |  |
| --- | --- | --- |
| Markers use only | | |
| Question | Maximum | Mark |
| 9 | 6 |  |
| 10 | 6 |  |
| 11 | 6 |  |
| 12 | 9 |  |
| 13 | 7 |  |
| 14 | 6 |  |
| 15 | 8 |  |
| 16 | 10 |  |
| 17 | 9 |  |
| 18 | 7 |  |
| 19 | 10 |  |
| 20 | 6 |  |
| 21 | 8 |  |
| S2 Total | 98 |  |
| S2 Wt (×0.6633) | 65% |  |

## Instructions to candidates

1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.

2. Write your answers in this Question/Answer booklet.

3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.

4. Additional working space pages at the end of this Question/Answer booklet are for planning or continuing an answer. If you use these pages, indicate at the original answer, the page number it is planned/continued on and write the question number being planned/continued on the additional working space page.

5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.

6. It is recommended that you do not use pencil, except in diagrams.

7. The Formula sheet is not to be handed in with your Question/Answer booklet.

Section Two: Calculator-assumed 65% (98 Marks)

This section has**thirteen (****13)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 100 minutes.

Question 9 (6 marks)

An exam has two parts, and , containing 15 and 8 questions respectively.

Determine the number of different combinations of questions a candidate could choose if they must answer

(a) 5 questions from part and 4 questions from part . (2 marks)

(b) 3 questions, all chosen from the same part. (2 marks)

(c) 3 questions, with at least one question from each part. (2 marks)

Question 10 (6 marks)

(a) The point is translated by the column vectors and to . Determine the values of the constants and . (2 marks)

(b) Determine the single matrix that represents, in order, the composition of a reflection in the line followed by a rotation of about the origin. Express matrix coefficients in exact form. (4 marks)

Question 11 (6 marks)

(a) A circle property says that if chords of a circle are of equal length then they subtend equal angles at the centre.

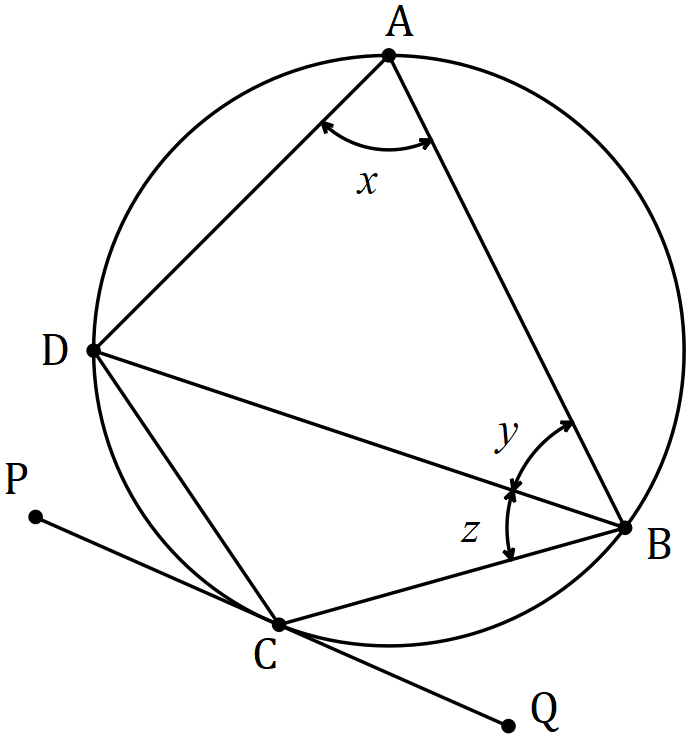
(i) Write the inverse of this statement. (1 mark)

(ii) Draw a diagram to illustrate the inverse statement and state whether it is true.

(2 marks)

(b) The diagram below shows four points , , and lying on the circumference of a circle. The line is a tangent to the circle at , , and .

Determine the size of angles , and . (3 marks)



Question 12 (9 marks)

(a) If and determine

(i) the angle between the directions of and , to the nearest tenth of a degree.

(2 marks)

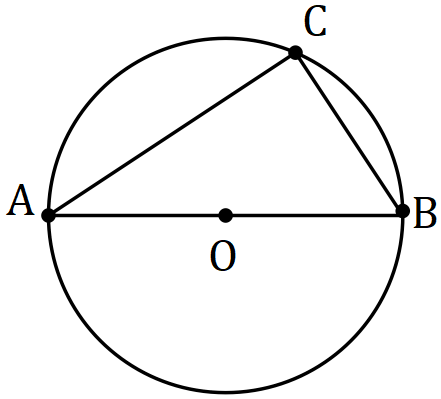
(ii) the scalar projection of on . (2 marks)

(b) The vector has a magnitude of and is perpendicular to the vector . Determine the values of the constants a and b, where . (5 marks)

Question 13 (7 marks)

(a) Point lies on the circumference of a circle with diameter cm, so that . Determine the exact length . (3 marks)

(b) Use a vector method to prove that the angle in a semi-circle is a right-angle. (4 marks)



Let and .

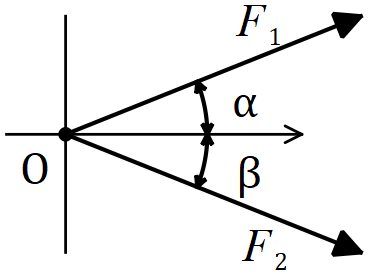
Question 14 (6 marks)

(a) Prove that . (4 marks)

(b) Hence, or otherwise, solve . (2 marks)

Question 15 (8 marks)

In the diagram below, forces and act on a body at the origin.

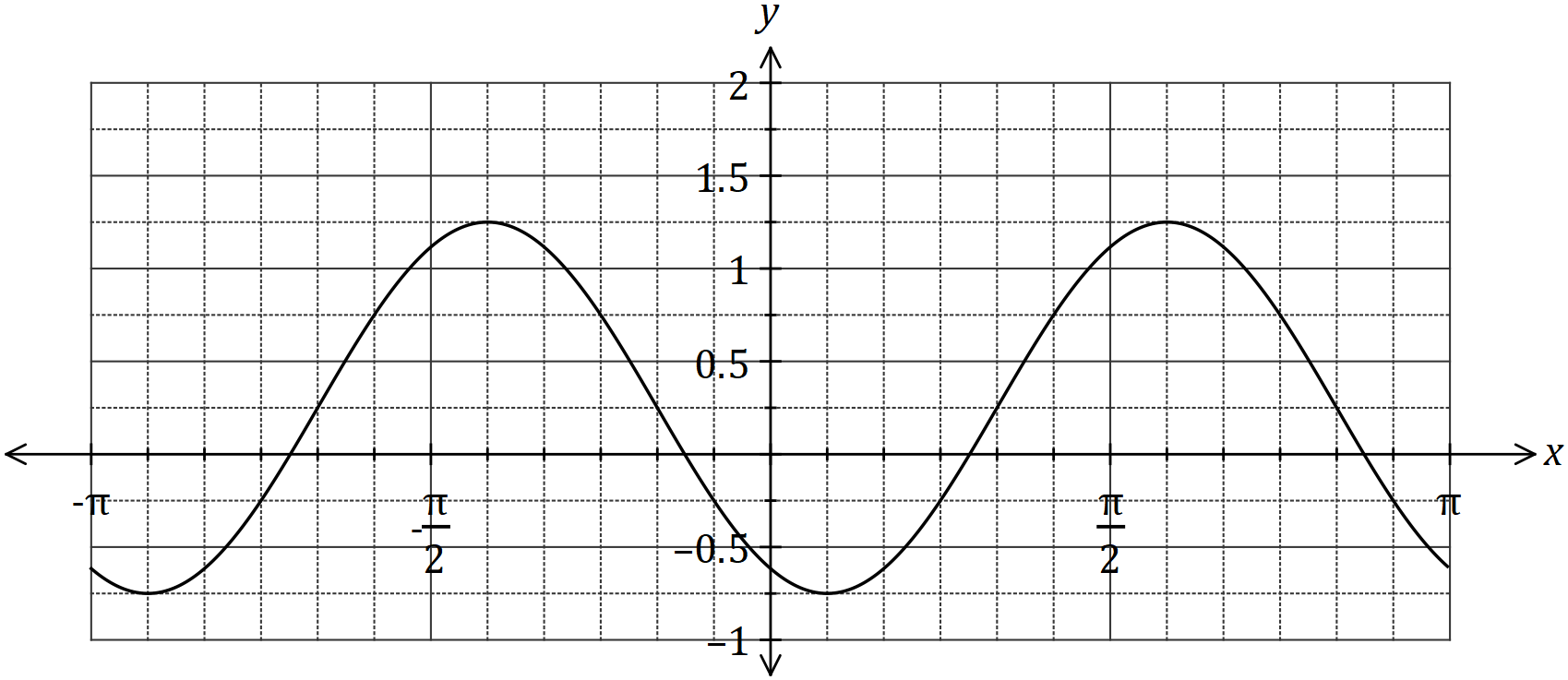


(a) If , , and , determine the magnitude of the resultant force and the angle it makes with the positive axis. (5 marks)

(b) If and , determine the angles and so that the resultant force is directed along the positive axis and has a magnitude of . (3 marks)

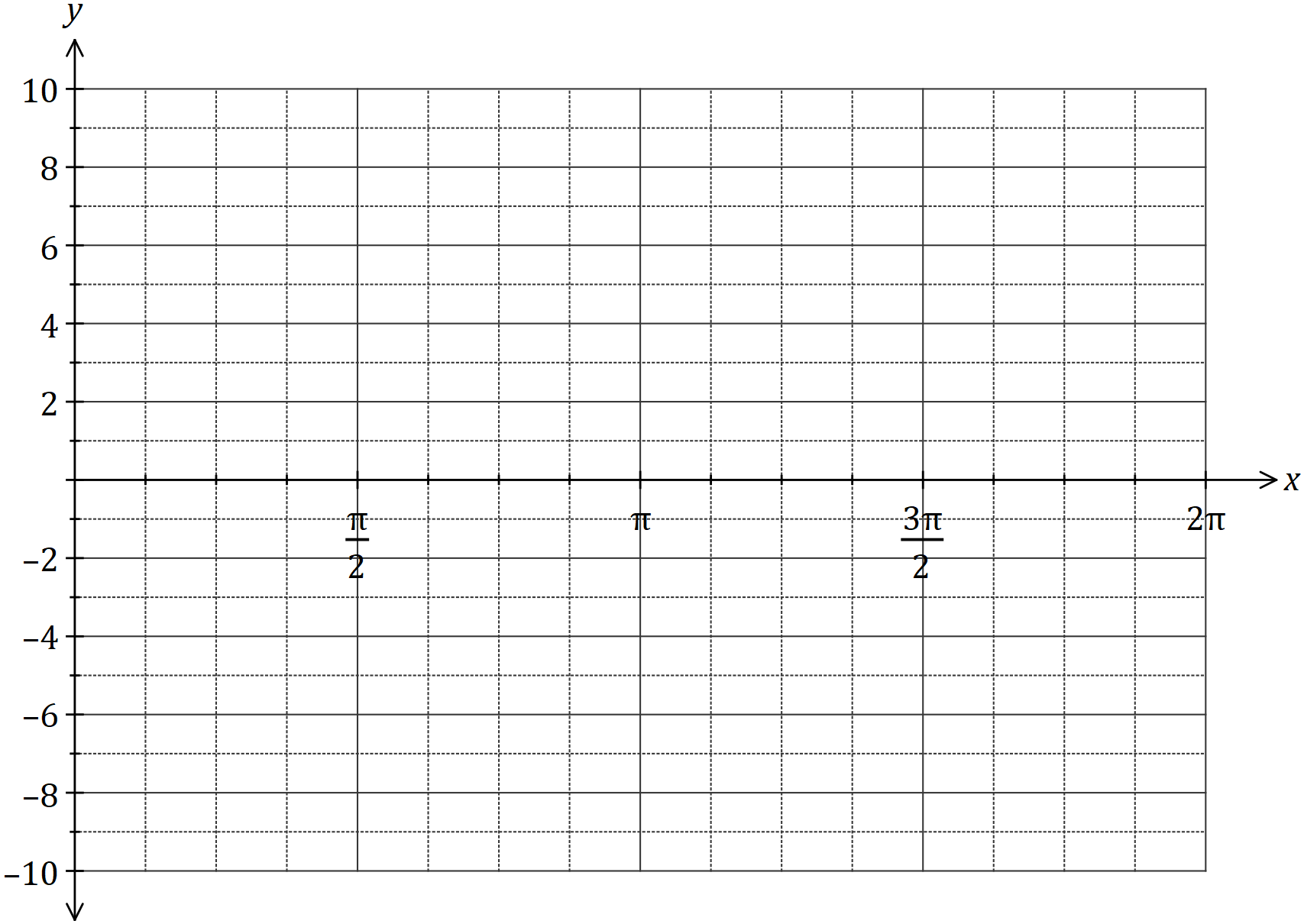
Question 16 (10 marks)

(a) The graph of is shown below for .



Determine the value of the positive constants , and . (3 marks)

(b) On the axes below, sketch the graph of , . (3 marks)



(c) The displacement, cm, of a particle from a fixed point varies with time, seconds, according to the model . Determine

(i) the initial displacement of the particle from . (1 mark)

(ii) the exact amplitude of the motion. (1 mark)

(iii) the period of motion. (1 mark)

(iv) the first time that the particle passes through , rounded to two decimal places.

(1 mark)

Question 17 (9 marks)

Triangle has vertices , and .

(a) The vertices are transformed to using matrix . Write down the new coordinates of the vertices and describe the transformation. (4 marks)

(b) The vertices are transformed to using matrix so that the new coordinates of the vertices are , and .

(i) Determine the transformation matrix . (3 marks)

(ii) If the area of triangle is square units, express the area of triangle in terms of . (2 marks)

Question 18 (7 marks)

(a) How many numbers must be chosen from the set of integers between 1 and 2017 inclusive to be certain that one of the numbers chosen is a multiple of 10. (3 marks)

(b) A number is formed using four different digits chosen from those in the number 23 814. Determine how many different numbers can be formed that are

(i) even. (1 mark)

(ii) greater than 8 000. (1 mark)

(iii) even or greater than 8 000. (2 marks)

Question 19 (10 marks)

(a) Trapezium has parallel sides and . is the midpoint of and lies on so that .

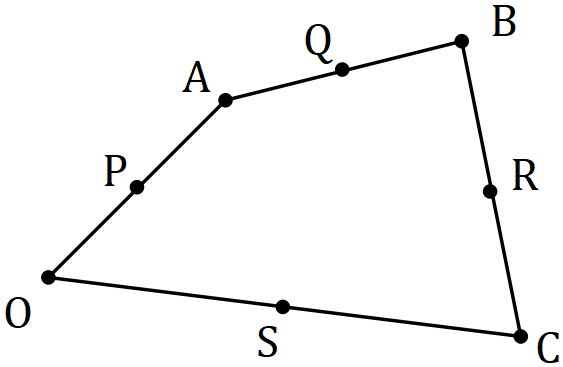
Given that , and , determine the following in terms of and .

(i) . (2 marks)

(ii) . (2 marks)

(iii) . (2 marks)

(b) Quadrilateral is shown below, where , , and are the midpoints of the sides , , and respectively. Let , and .

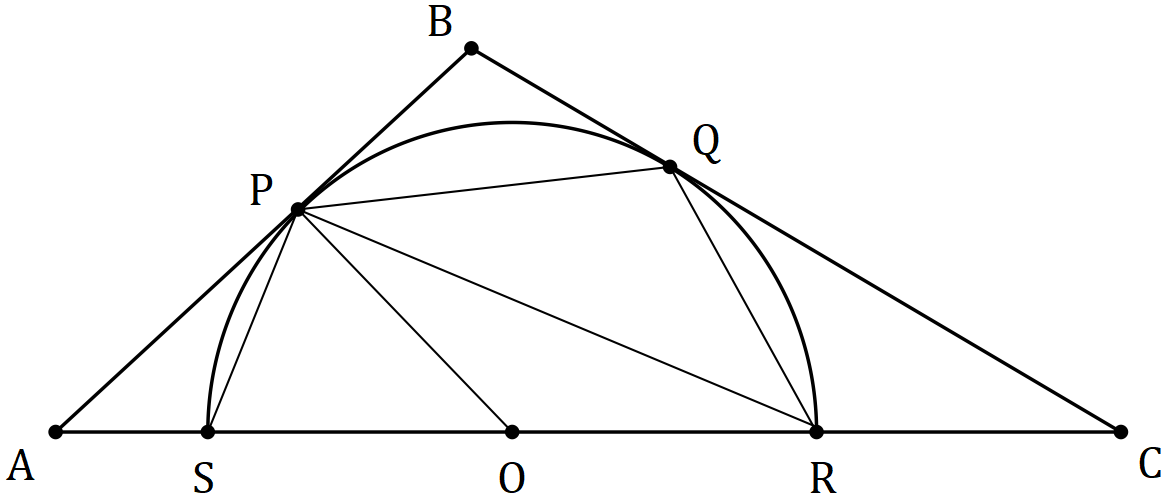


Show that . (4 marks)

Question 20 (6 marks)

The diagram shows a semi-circle, with diameter and centre , circumscribed by triangle , in which and .

Determine, with reasons, the size of angles and .



Question 21 (8 marks)

The sum of the first terms of the sequence is .

(a) Show that this statement is true when . (2 marks)

(b) Use mathematical induction to prove the statement is true for . (6 marks)

Additional working space

Question number: \_\_\_\_\_\_\_\_\_

Additional working space

Question number: \_\_\_\_\_\_\_\_\_

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